

## LESSON 2/3 – PHYSICS AND TECHNOLOGY OF PRINTING

*Prof. Vivek Subramanian*

### Why print?

- Low cost?



Courtesy:  
G. Cho,  
Sunchon National University

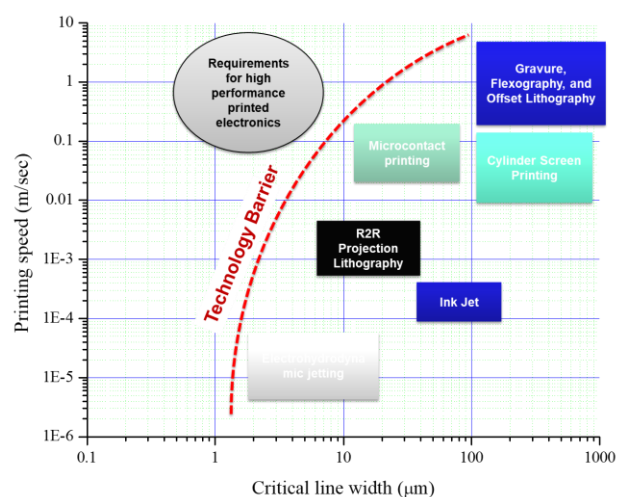
- Added functionality

- Integration – spatially specific deposition
- Customizability – digital printing
- Lightweight / robust / flexible

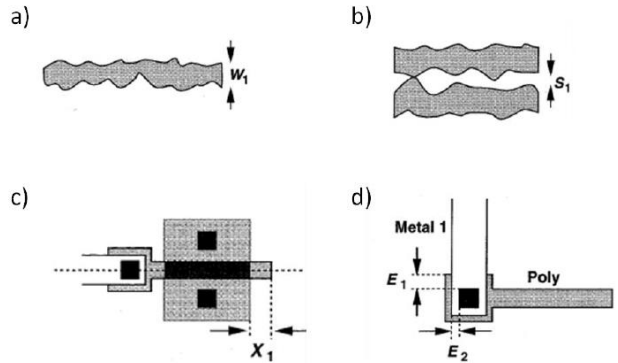
## General tradeoffs in printing

- **Resolution:** Printing techniques vary widely in resolution from nm (nanoimprint) to 100 $\mu$ m (high-speed screen)
- **Speed:** Traditional analog printing techniques (screen, gravure, offset) are exceedingly fast (100's of m/min), while nanoimprint is immature, and probably too slow for printed electronics
- **Viscosity:** Electronic materials often have limited viscosity ranges. Offset printing requires very high viscosity inks (like toothpaste), while digital techniques such as inkjet can work with low viscosities (e.g., alcohols)

## Resolution trade-offs in Printing



## Pattern fidelity requirements

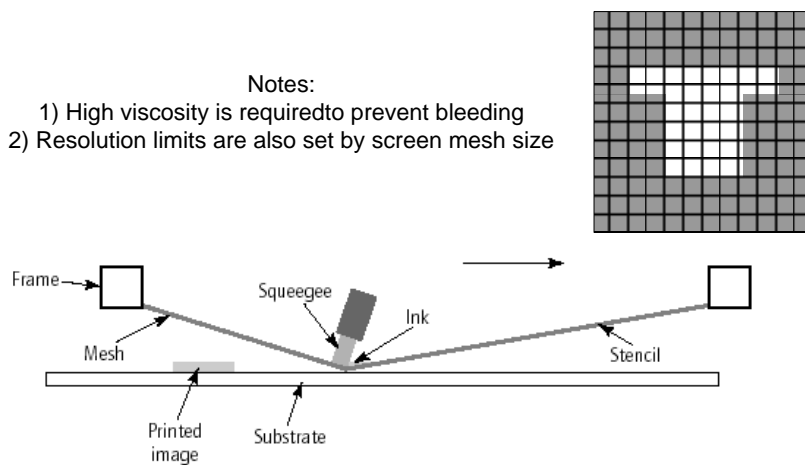


Consider:

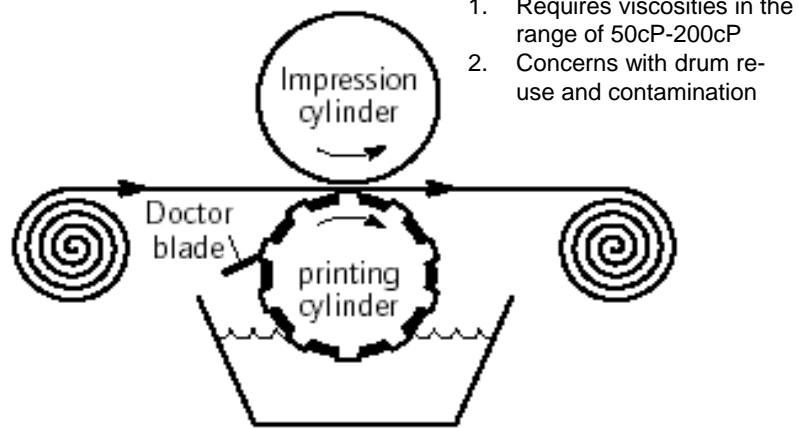
- Line edge roughness
- Line-space roughness
- Overlay

## Screen Printing

- Notes:
- 1) High viscosity is required to prevent bleeding
  - 2) Resolution limits are also set by screen mesh size

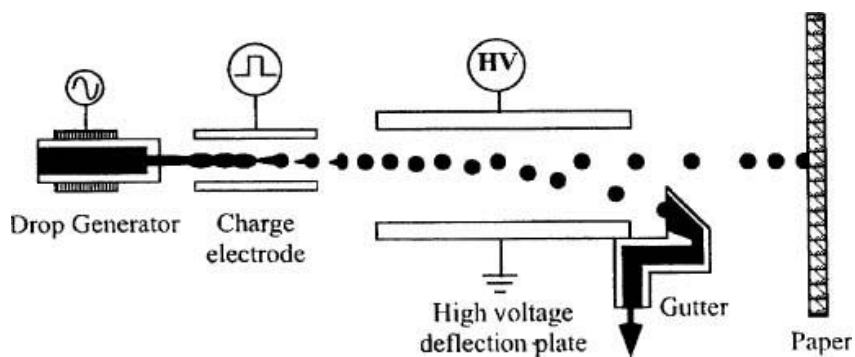


## Gravure Printing



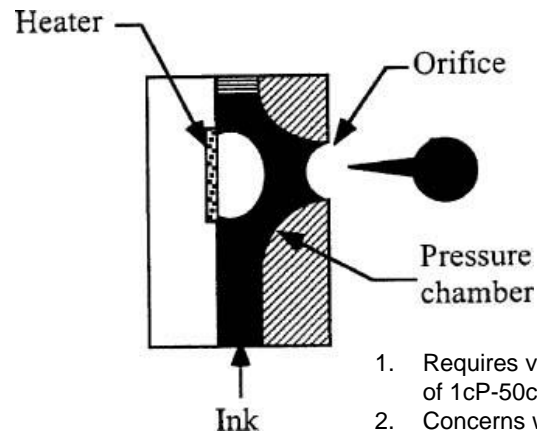
1. Requires viscosities in the range of 50cP-200cP
2. Concerns with drum re-use and contamination

## Continuous Inkjet Printing



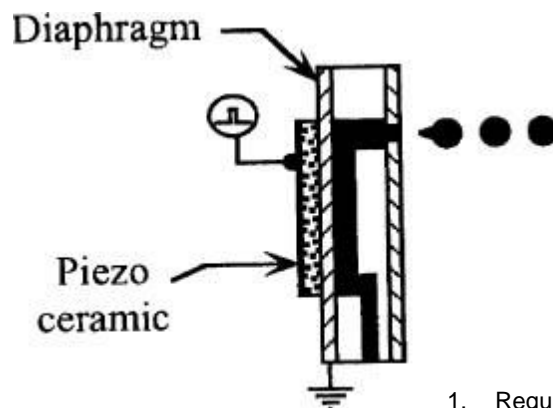
1. Requires viscosities in the range of 5cP-50cP
2. Concerns with ink wastage and contamination

## Thermal Inkjet Printing



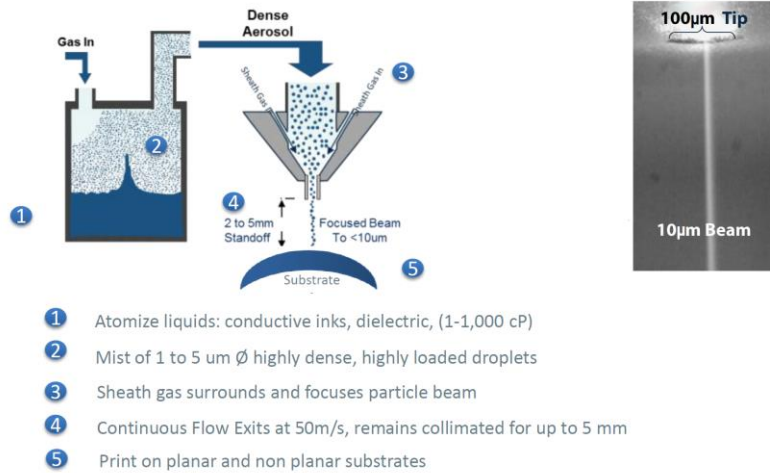
1. Requires viscosities in the range of 1cP-50cP
2. Concerns with ink degradation and compatibility

## Piezo Inkjet Printing

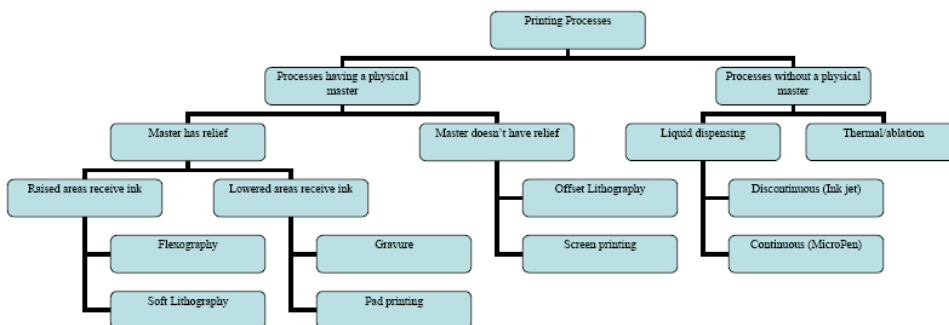


1. Requires viscosities in the range of 1cP-50cP
2. Concerns with manufacturability

## Aerosol jet



## Taxonomy of printing processes

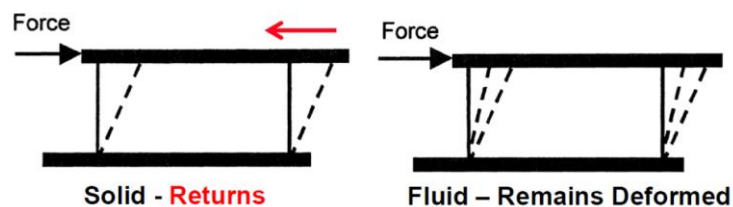


## Choosing a print technique

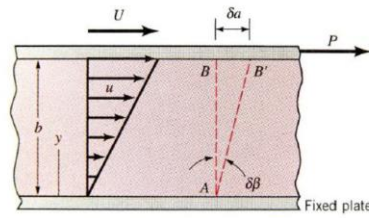
- **Materials Properties**
  - Viscosity
  - Surface Tension
- **Physical Requirements**
  - Resolution
  - Registration
  - Thickness
- **Economics**
  - Throughput
  - Master / Plate costs
  - Waste
  - Material Costs

## What is a fluid

- A fluid is any substance that deforms continuously under the application of shear stress of any magnitude
- Gasses and liquids
- Newtonian liquid

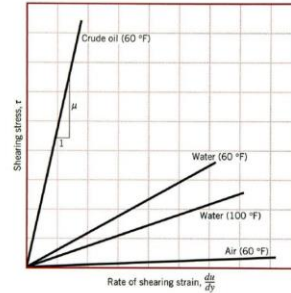


## Viscosity



$$\tau = \mu \frac{du}{dy}$$

where  
 $\tau$  is the **shearing stress**  
 $\mu$  is the **absolute dynamic viscosity**  
 $\frac{du}{dy}$  is the **velocity gradient**



In addition:

$$\mu \sim \mu_0 e^{-(T-T_0)}$$

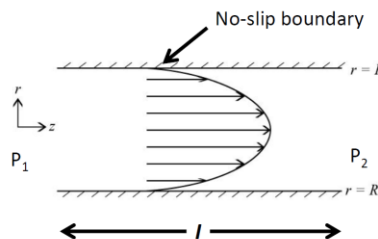
Thermal effects

## Fluid flow through a pipe

### Poiseuille's equation and scaling

For a fluid passing through a tube, the Navier-stokes equation implies

$$V = \frac{\pi(P_1 - P_2)r^4}{8\mu l}$$



For narrow pipes the flow rate (V) is strongly reduced.

#### Household pipes

$\Delta P=3$  bar,  $R=5$  cm  
 $\mu=0.01$  poise,  $L=10$  m  
 $V=73$  m/s

#### Washing machine

$\Delta P=3$  bar,  $R=1$  cm  
 $\mu=0.01$  poise,  $L=5$  m  
 $V=0.2$  m/s

#### Ink-jet printer

$\Delta P=3$  bar,  $R=100$   $\mu$ m  
 $\mu=0.01$  poise,  $L=5$  cm  
 $V=20$   $\mu$ m/s



## The Reynolds number

- The Reynolds number is a ratio between the internal forces in a fluid and the viscous forces

$$Re = \frac{\rho V D}{\mu}$$

Where  
 $\rho$  is the fluid density  
 $V$  is the fluid velocity  
 $D$  is the pipe diameter  
 $\mu$  is the viscosity



Osborne Reynolds  
 Born Belfast 1842  
 First UK "Professor of Engineering"

### Re < 2100

- Laminar (Stokes) flow
- Slow fluid flow
- No inertial effects
- Heavy damping

### Re > 4000

- Unstable laminar flow
- Turbulent flow

## The Reynolds number in inkjet printing

### Household pipes

$\Delta P = 3$  bar,  $R = 5$  cm  
 $\mu = 0.01$  poise,  $L = 10$  m  
 $V = 73$  m/s

### Washing machine

$\Delta P = 3$  bar,  $R = 1$  cm  
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### Ink-jet printer

$\Delta P = 3$  bar,  $R = 100$   $\mu$ m  
 $\mu = 0.01$  poise,  $L = 5$  cm  
 $V = 20$   $\mu$ m/s

Water density =  $10^3$  kg.m<sup>3</sup>  
 Viscosity =  $10^{-3}$  kg.s<sup>-1</sup>.m<sup>-1</sup>

Re =  $3.65 \times 10^6$

Re = 2000

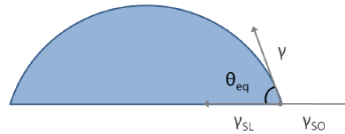
Re =  $2 \times 10^{-4}$

- For most flow rates and small pipes Re is small and the flow is laminar
- Viscosity is dominant and we are in the realm of Microfluidics!

## Liquids on surfaces: Some basic discussion

$$\gamma \cos \theta_{eq} = \gamma_{SL} - \gamma_{SO} \quad (1)$$

The fluid's surface tension is  $\gamma$ , and  $\gamma_{SL}$  and  $\gamma_{SO}$  represent the substrate-liquid and substrate-air interfacial tensions, respectively.



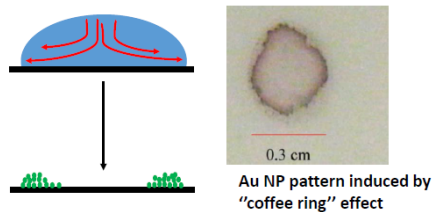
The substrates in this work are rough and have defects, and the printed inks dry and deposit solute. For both of these reasons, the contact line's advancing ( $\theta_{adv}$ ) and receding ( $\theta_{rec}$ ) contact angle separate in value leading to contact-angle hysteresis. The contact line is stable when  $\theta_{rec} < \theta < \theta_{adv}$ , else it retreats or advances as appropriate. Evaporating colloidal inks often have zero retreating contact angle and are said to have pinned contact lines that may advance but never retreat.

## Effects with real inks

### "Coffee Ring" Effect and Marangoni Flow

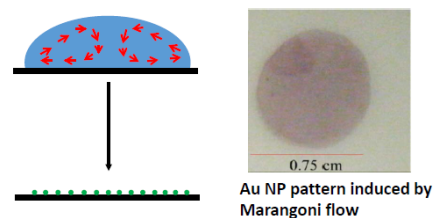
- During solution evaporation, there are two major competing evaporation-driven effects, "coffee ring" effect and Marangoni flow.

#### "Coffee ring" Effect



- Dense, ring-like structure along the perimeter
- 1) Absence of circulating flow
  - 2) Contact line of drying droplet is pinned
  - 3) Outward flow carries solutes to the periphery

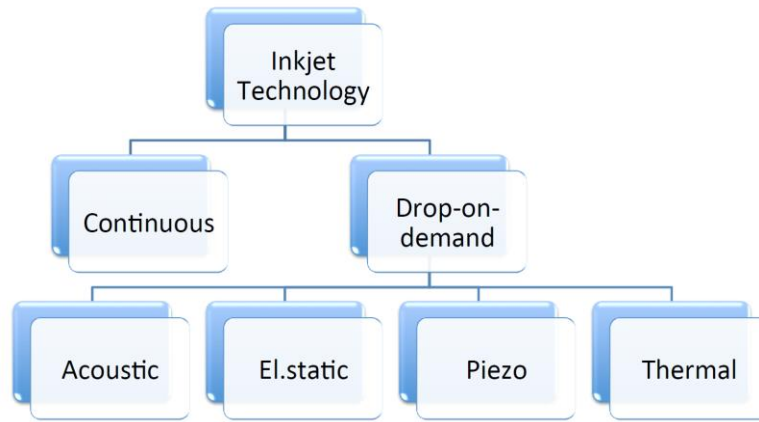
#### Marangoni Flow



Ordered structure across the surface

The surface tension driven flow carries particles inward toward the top of the droplet and then plunges them downward where they can either adsorb onto the substrate near the center of the droplet or be carried along the substrate to the edge, where they are re-circulated along the free surface back toward the top of the droplet.

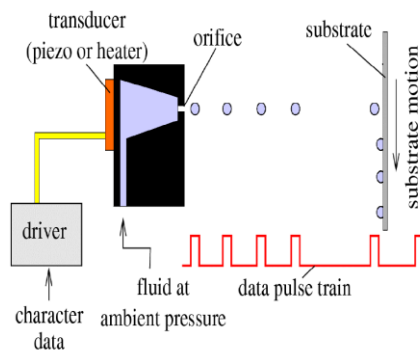
## Taxonomy of major inkjet technologies



## Droplets on demand inkjet printing

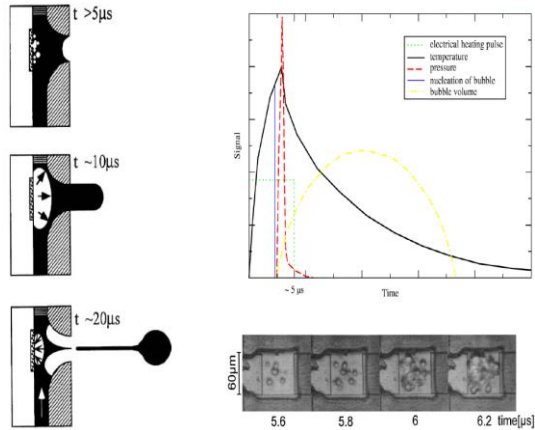
- Mechanism of droplet formation:

- Thermal
- Piezo-electric
- Electrostatic
- Acoustic



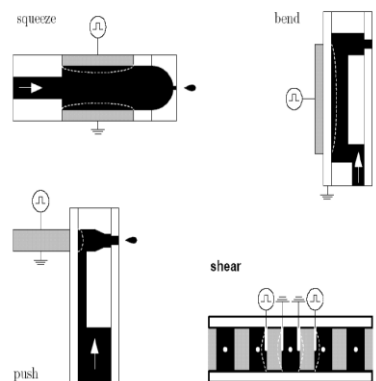
## Thermal inkjet printing

- Phase of droplet formation
- Heating
  - Overheated ink (over the spinodal limit, around 300°C for water)
  - At 300°C: nucleation of bubble
- Expansion
  - Ejection of ink
  - Parallel to bubble expansion
- Droplet formation
  - Collapsing vapour bubble
  - Retraction of bulk ink
  - Refilling of cavity (80-200 us, speed critical step)



## Piezo inkjet printing

- Deformation of piezo-ceramics
- Change in volume
- Pressure wave propagates to nozzle
- Deflection of piezo-ceramics in submicrometric range
- Piezo-element has to be much larger than orifice
- Main problem: miniaturization



## Droplet formation in piezoelectric inkjet printers

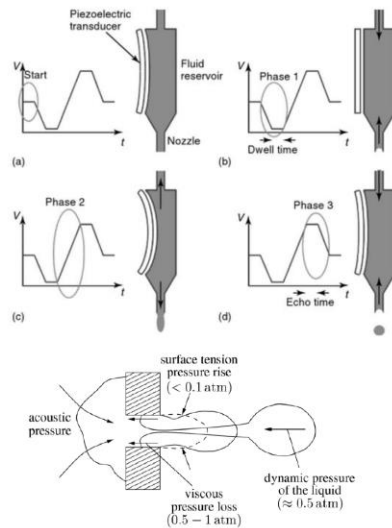
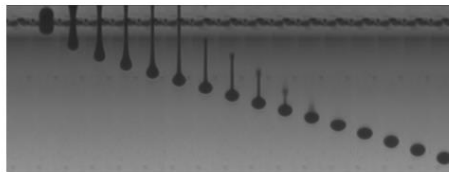
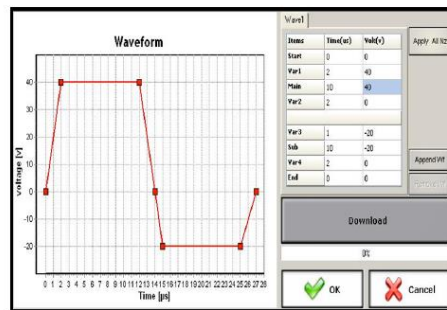


Fig. 8.5. Pressures governing the ejection dynamics of a liquid jet out of a nozzle

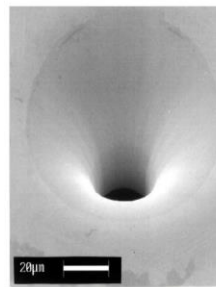
- Starting deflection
- Ink influx & meniscus formation
- Acoustic  $\rightarrow$  kinetic energy  
high velocity jet from nozzle
  - Viscous pressure loss
  - Negative pressure wave reflection
  - Drop formation
- Cavity relaxation period & meniscus formation

## Example: typical bipolar waveform

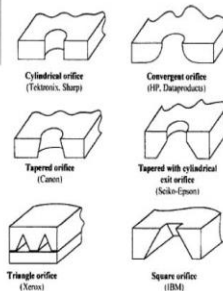


## Nozzle design

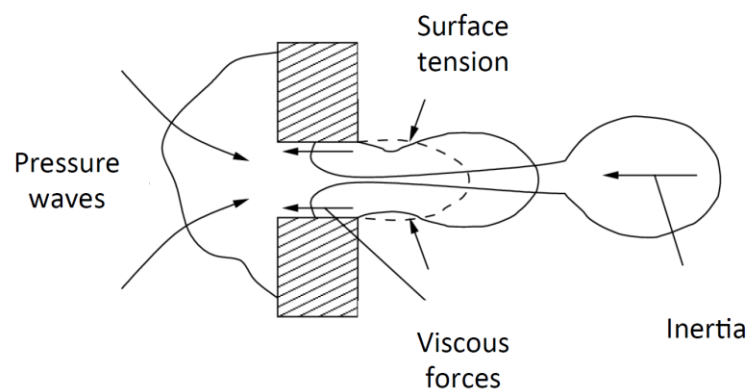
- Geometry parameters of nozzle
  - Diameter
  - Depth
- Effect on droplets
  - Volume
  - Speed
  - Deflection angle
- Effect on ink supply (refilling)
  - Capillary forces
- Fabrication tolerances limit picture quality
- Fabrication of orifice plates
  - Laser-ablation in polyimide, especially for small nozzles (10  $\mu$ l, 20  $\mu$ m)
  - Nickel-electroplating
  - Electro-discharge machining (EDM)
  - Micro-punching
  - Micro pressing



Electroplated Ni-nozzle



## Ink design considerations



## Ink formulation

The Weber number relates the balance between inertial and capillary forces in a fluid

$$We = \frac{\rho V^2 D}{\gamma}$$

Where  
 $\rho$  is the fluid density  
 $V$  is the fluid velocity  
 $D$  is the pipe diameter  
 $\gamma$  is the surface tension

The Ohnesorge number is the ratio of the Reynolds and Weber numbers

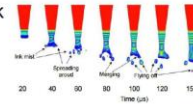
$$Oh = \frac{We^{1/2}}{Re}$$

Inverse ratio gives the Z index for inks

$$Z = Oh^{-1} = \frac{(D\rho\gamma)^{1/2}}{\mu}$$

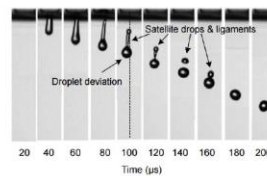
Numerical criteria for ink formulation

$Z > 2$  for successful printing  
 Viscosity large enough to dissipate acoustic → kinetic shock

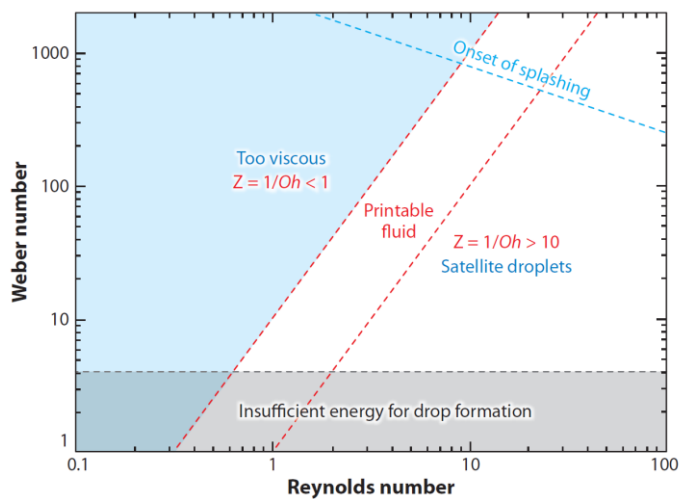


$Z < 70$

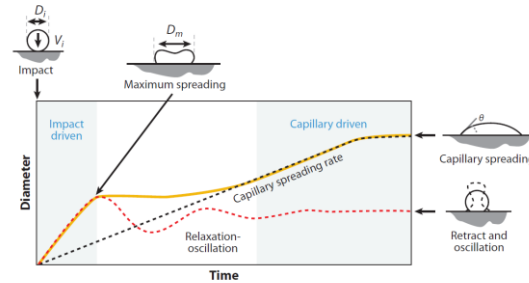
Satellite Droplets form separately to the main drop



## Drop ejection

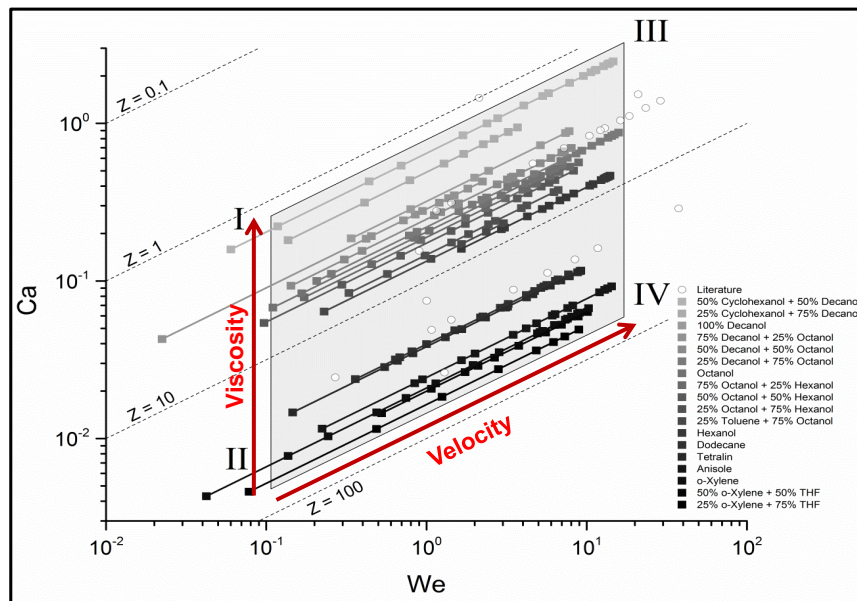


## Physics of drop: impact



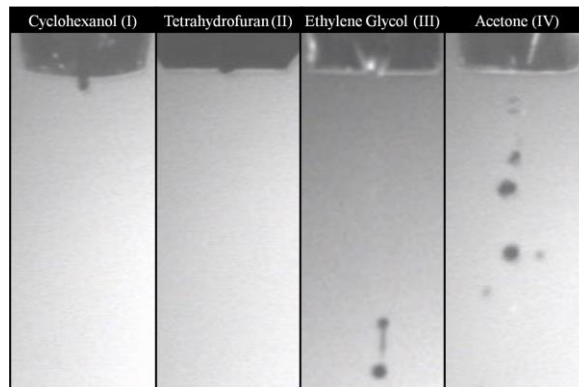
- The final diameter is a linear function  $D_i$
- The drop footprint increases with decreasing the contact angle and is about  $3D_i$  at a contact angle of  $10^\circ$
- Coffee ring effect

## Jettability Window





## Breakdown Mechanisms Observed



### Regions I and II:

- inertial force (driven by pulse amplitude) too low for drop ejection

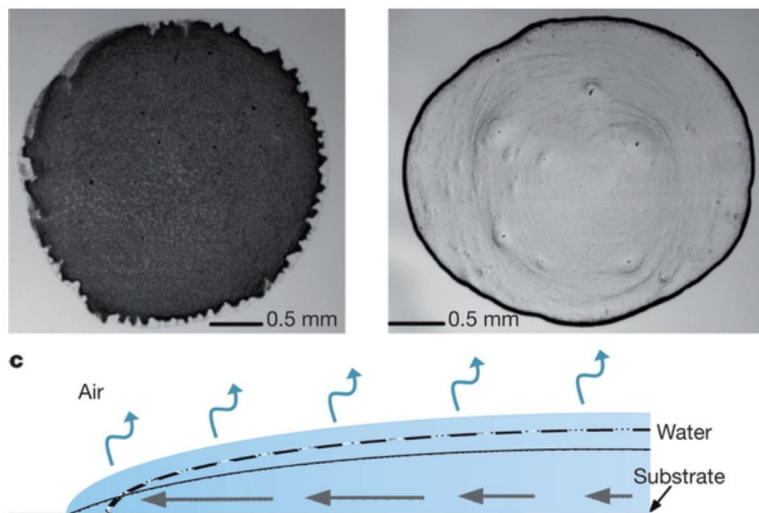
### Region III:

- emerging ink pillar too long → satellite drops form from tail of drop

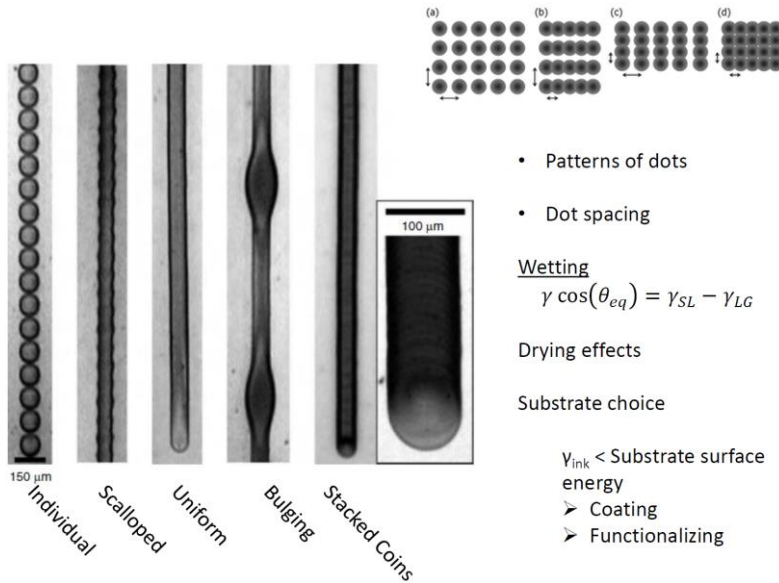
### Region IV:

- inviscid ink subjected to large inertial force → wavelike instability created → multiple breakups of drop tail

## Reminder: the coffee ring effect

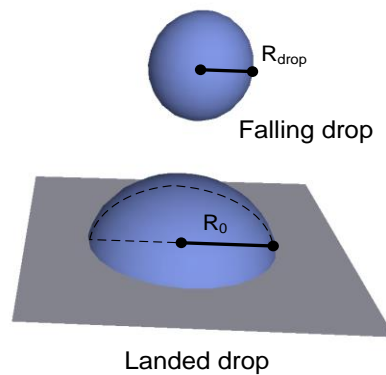


## Pattern formation



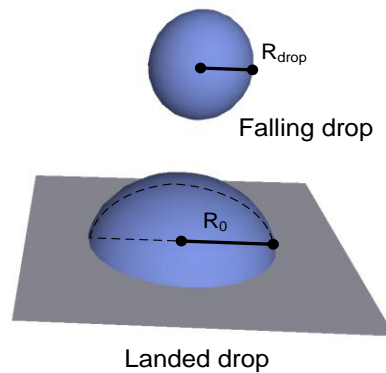
## So what causes these effects?

- Step 1: Drop hits the surface and expands to an impinging radius  $R_0$



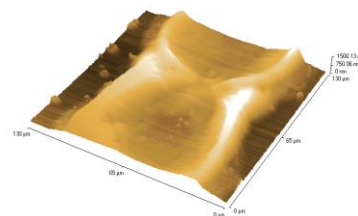
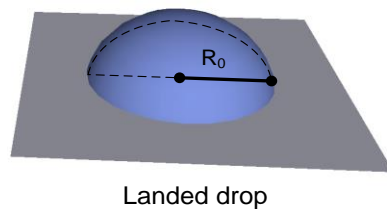
## So what causes these effects?

- Step 2: Edge of drop is “pinned”



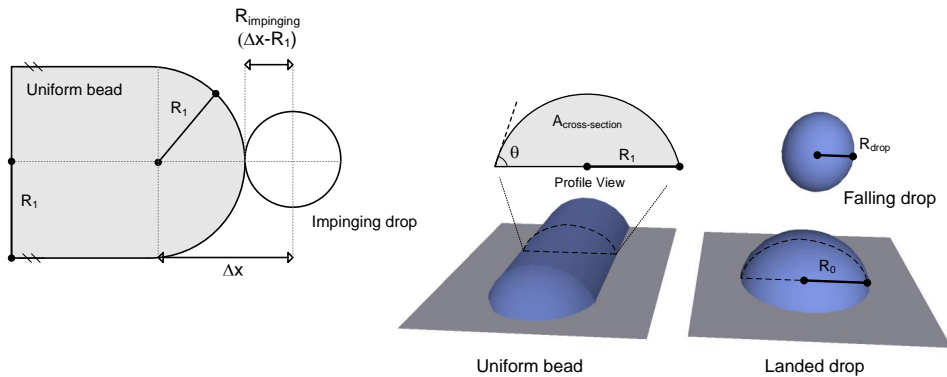
## So what causes these effects?

- Step 3: In isolated drops, drying causes:
  - Convective flow: edge is cooler than center, causing outward flow of material (coffee ring effect)
  - Marangoni effect: surface tension is temperature dependent, causing flow of material (can reverse coffee ring effect).
  - Final structure depends on relative rates



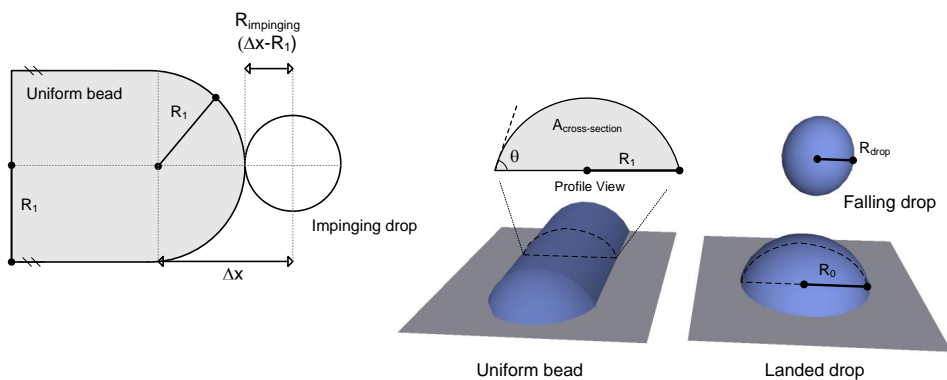
## What happens in lines?

- Step 1: Impinging drop “connects” to bead of line, and material flows back into line for same reason that coffee ring occurs



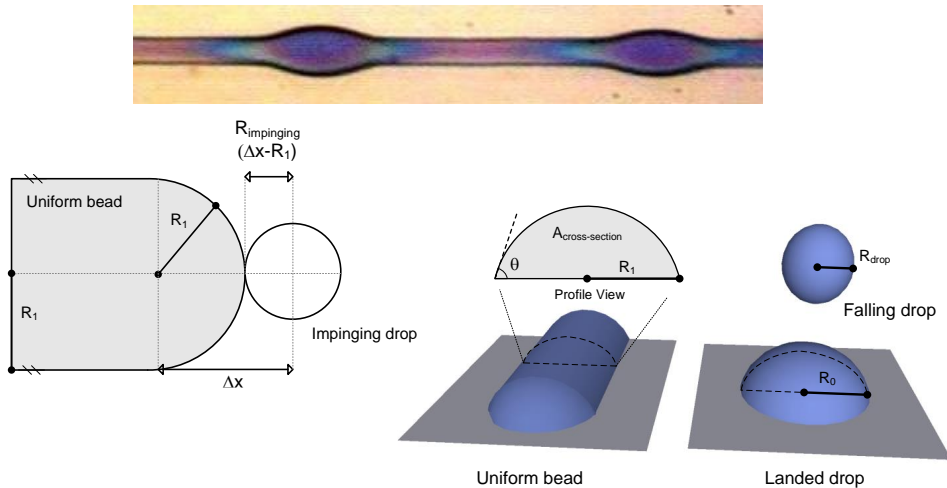
## What happens in lines?

- If flow is too slow, drop “dries” before line evens out, causing scalloping

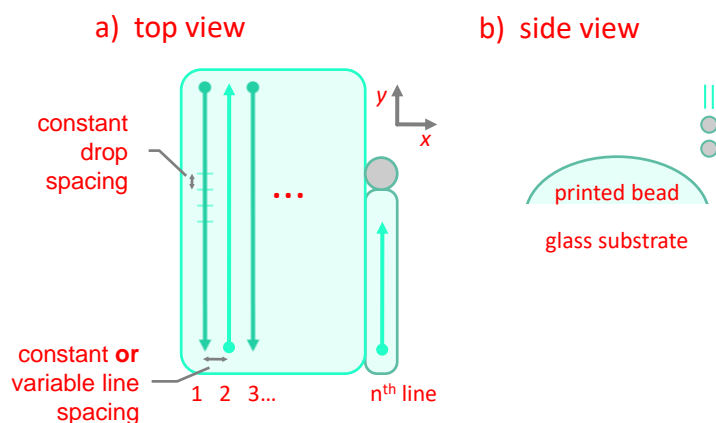


## What happens in lines?

- If flow is too fast, bead cannot absorb material fast enough, causing bulging



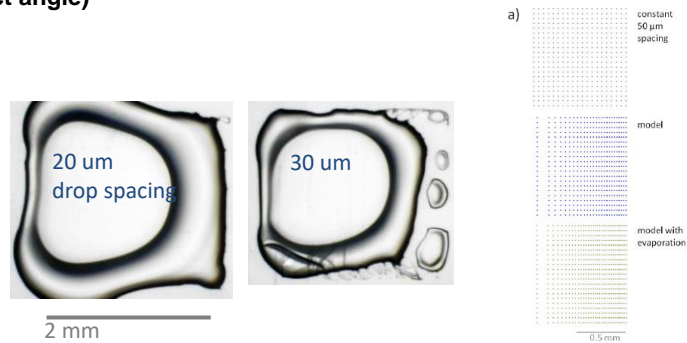
## Two dimensional shape generation



- As patterns are printed, the contact angle of the bead can go in and out of the steady-state zone... this leads to instabilities

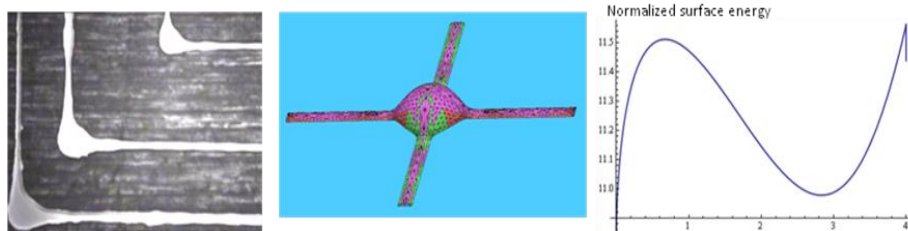
## Bulging and instability in two dimensions

- Dense drops cause bulging
- Sparse drops cause bead separation (since bead contact angle drops below receding contact angle)



- There is therefore an inherent limit to constant-space printing, which is what *all* existing tools tend to do.
- Solution: adjust drop spacing to control stability


## Instabilities in corners

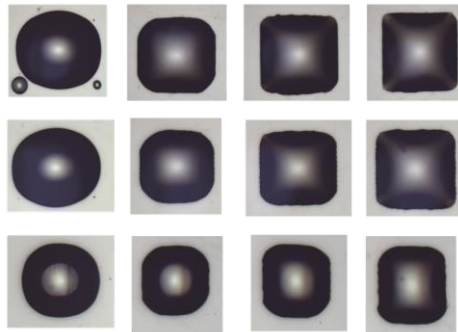


- Flow in corners can drive to formation of bulges
  - Can position to equilibrium that eliminates bulges by proper design of process
  - Can exploit bulge formation to cause linewidth shrinking... (more on this later)

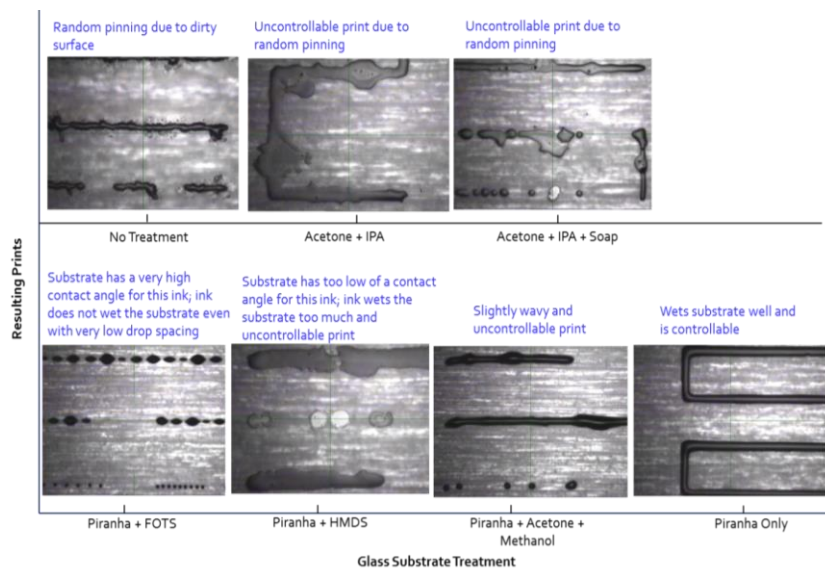
## The impact of the substrate

- E.g., controlled contact angle hysteresis

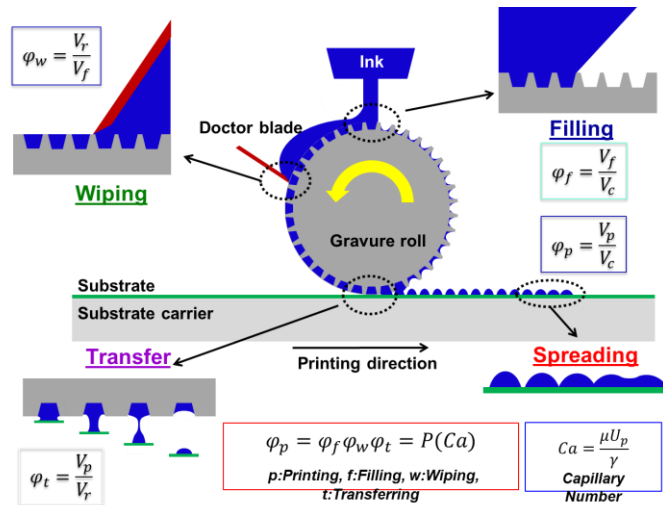
Increasing hysteresis (fixed  $\theta_A$ , decreasing  $\theta_S$ ) 



## Substrate Interactions

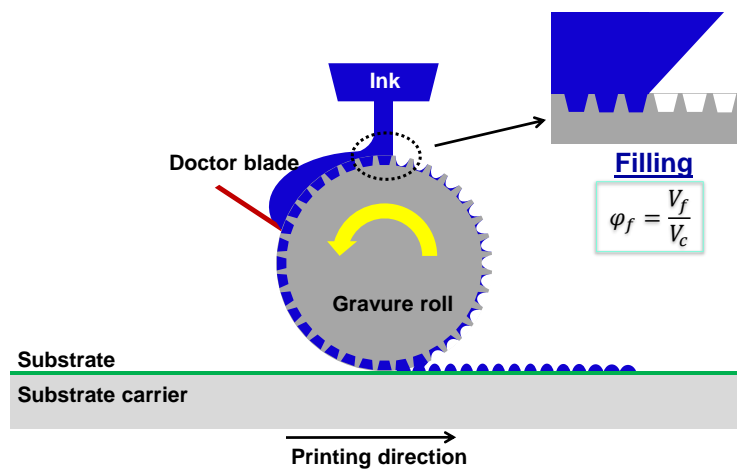


## Gravure Printing



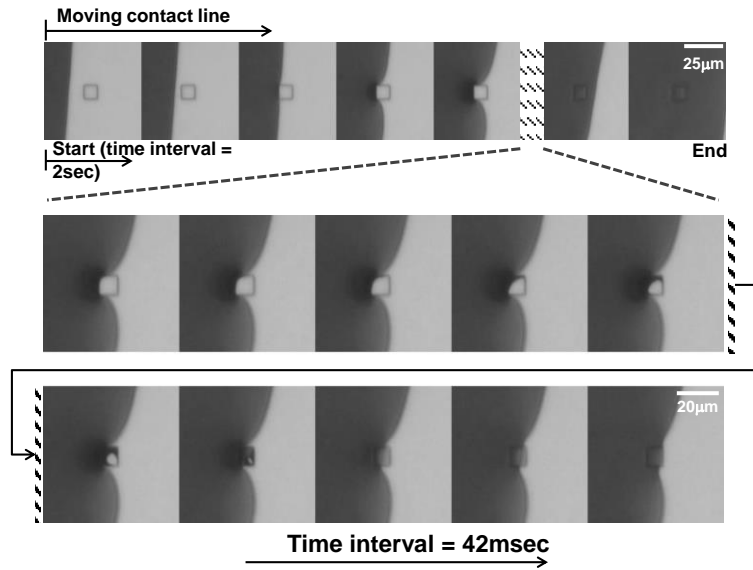
Kitsomboonloha, R., Morris, S. J. S., Rong, X., & Subramanian, V. (2012) *Langmuir*, 28(48), 16711–23

## Filling Process

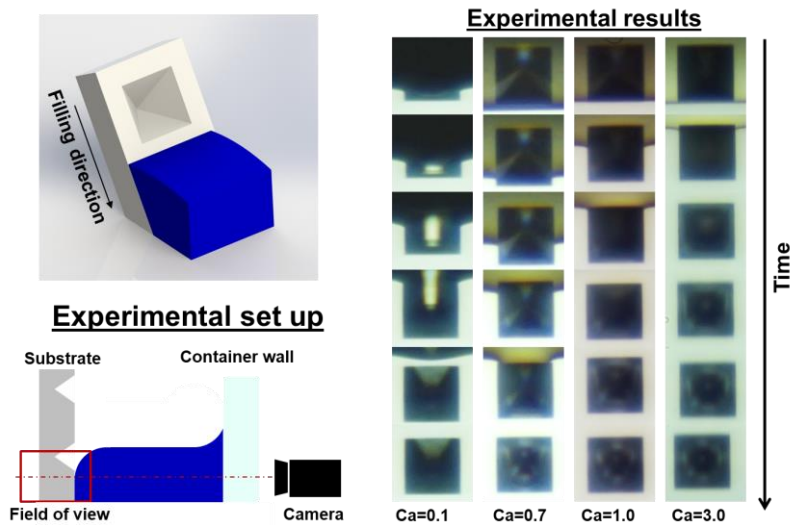




## Filling Mechanism

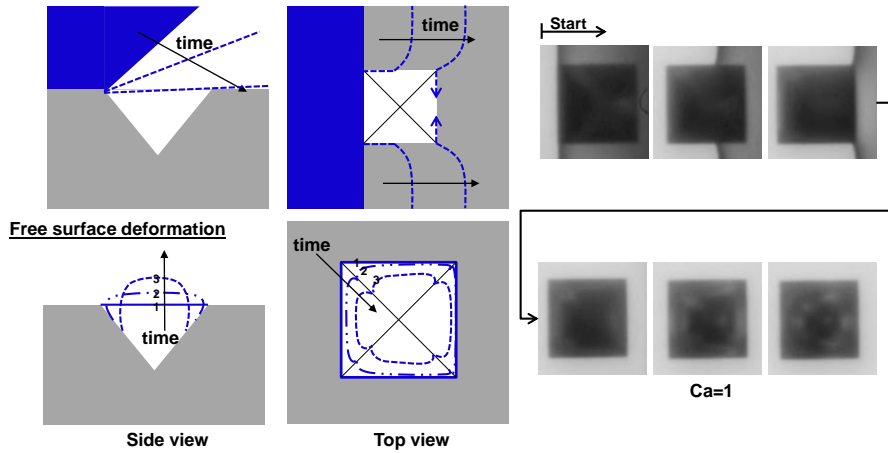


## Filling Mechanism



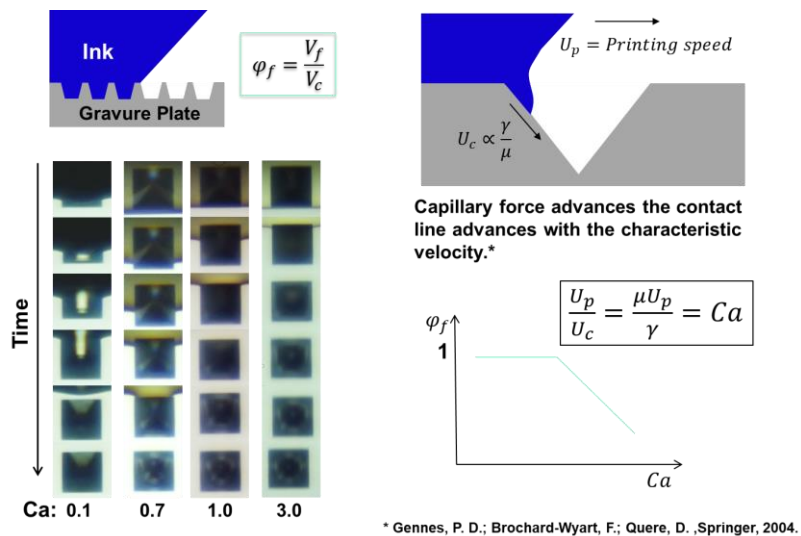
## Air entrapment

### Air entrapment

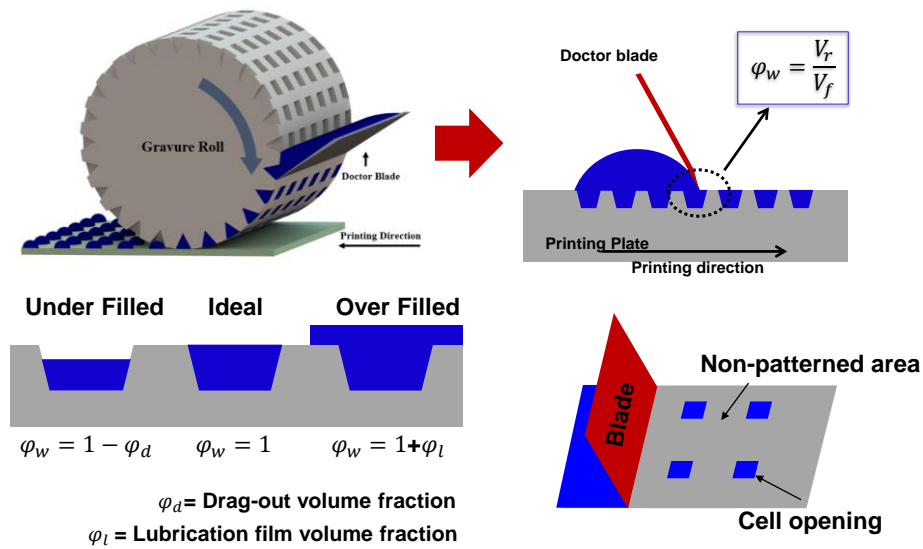


Assume perfect pinning at the cell edges

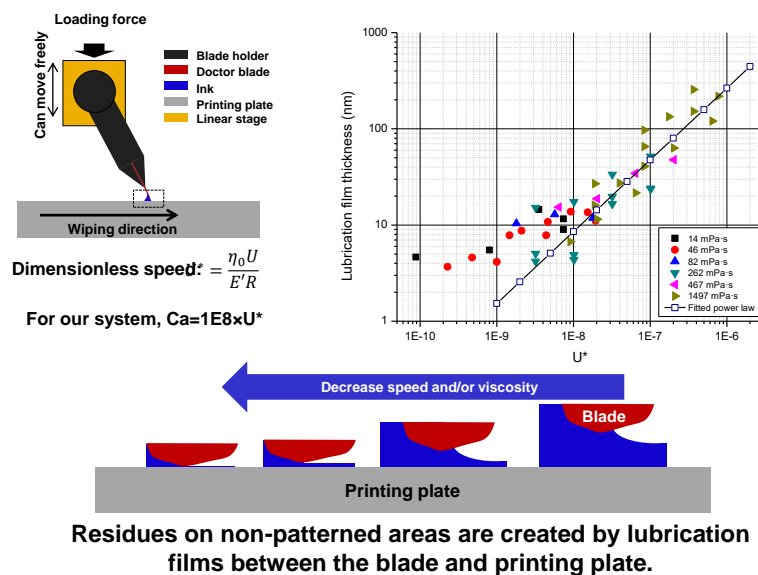
## Filled Volume Fraction



## Wiping Process



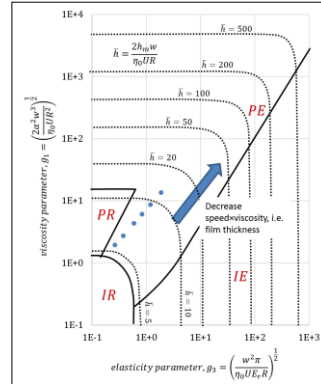
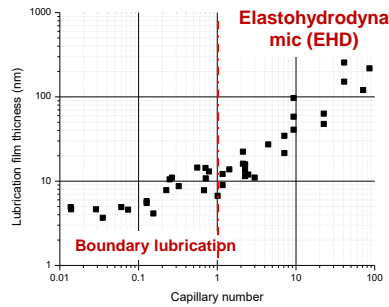
## Wiping on Non-patterned Areas



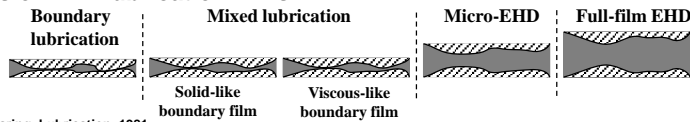
## Lubrication Films in Gravure

Film thickness<sup>1</sup>:  $h \propto U\eta^{0.67}$

Lubrication regimes<sup>3</sup>:



Regions of EHD lubrication films<sup>2</sup>:

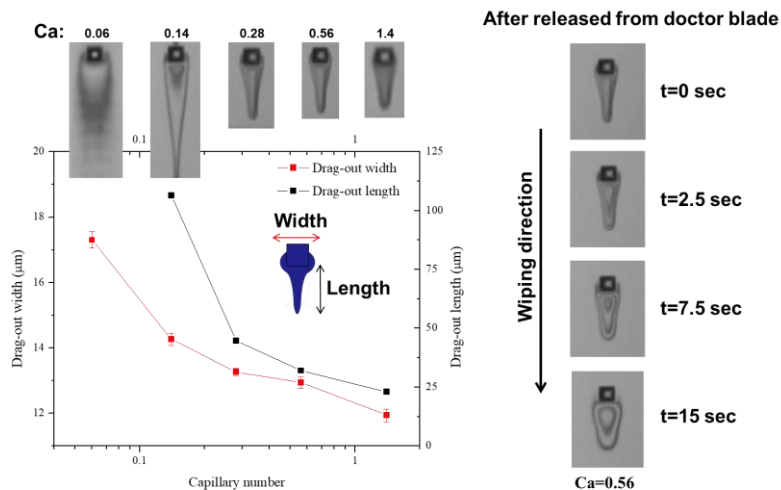


<sup>1</sup>Dowson, Ball Bearing Lubrication, 1981

<sup>2</sup>H. A. Spikes and A. V. Olver, "Basics of mixed lubrication," *Lubrication Science*, vol. 16, no. 1, pp. 1–28, Nov. 2003.

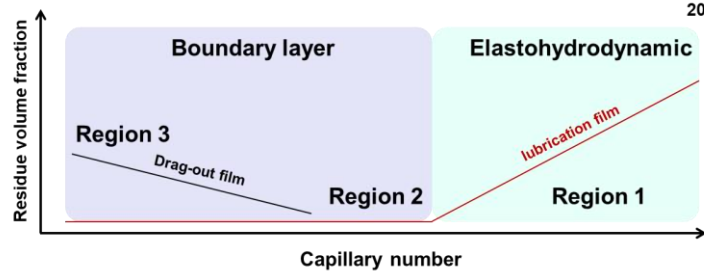
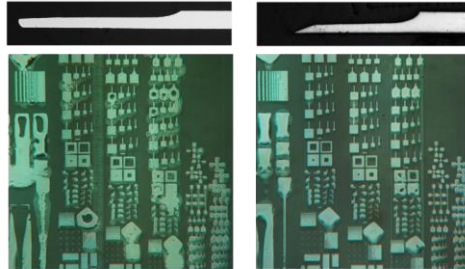
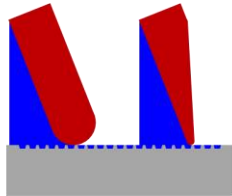
<sup>3</sup>Johnson, K. L., "Regimes of elastohydrodynamic lubrication", *Journal of Mechanical Engineering Science* 12(1), 9–16, 1970.

## Characteristic of Drag-out Tails

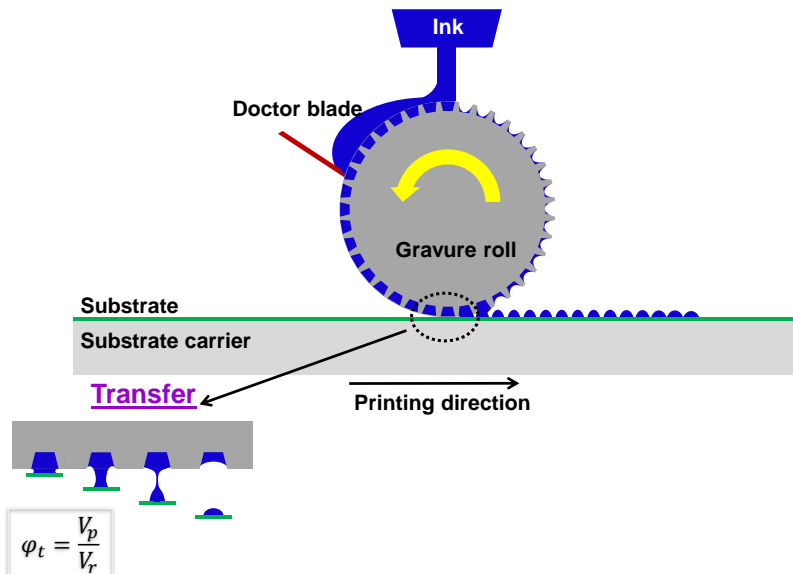


## Perfect Wiping

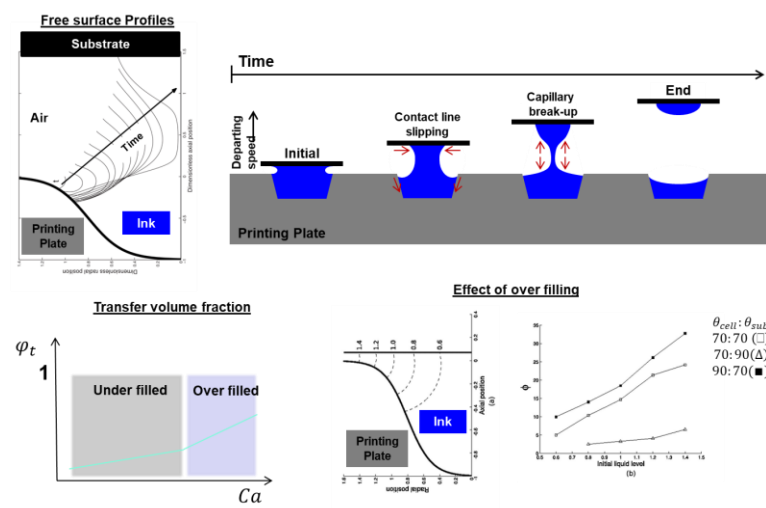
Optimization:  
-Printing condition  
-Blade geometry



## Transferring Process

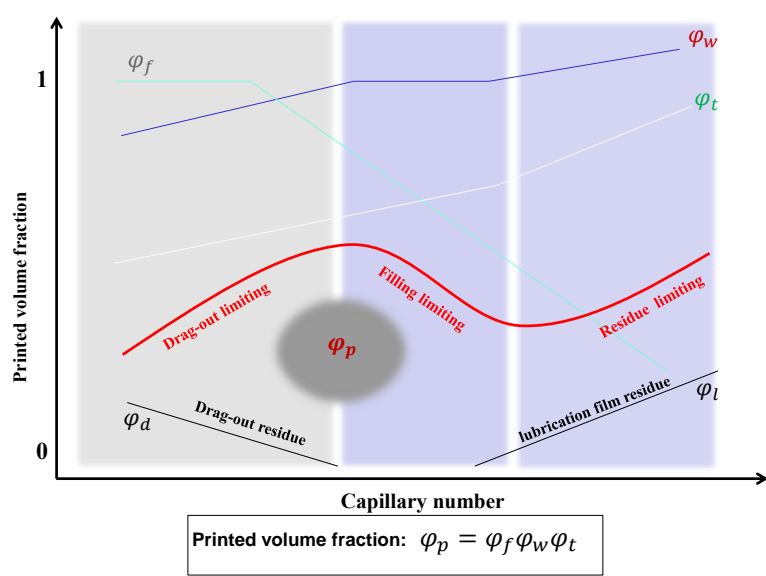


# Transfer Mechanism

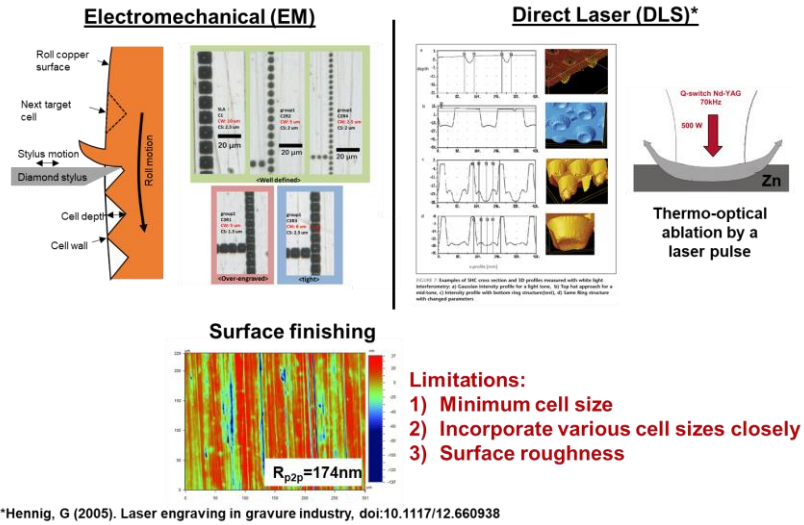


Shawn Dodds, Marcio da Silveira Carvalho, and Satish Kumar *Physics of Fluids* 21, no. 9 (2009): 092103

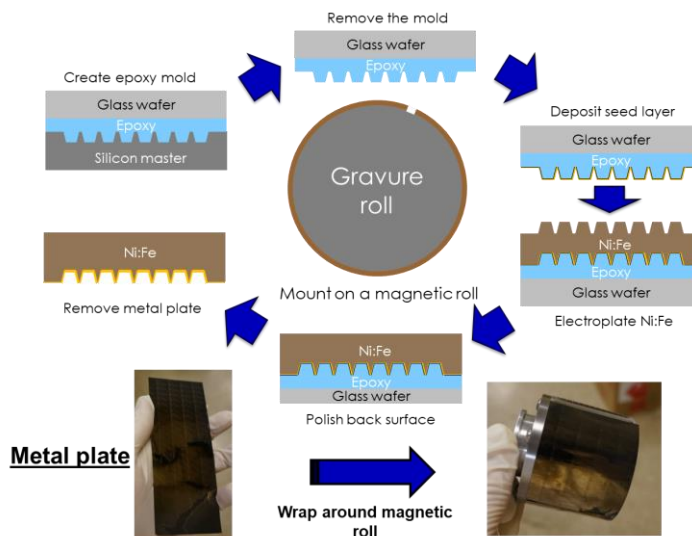
# Characteristic of Gravure Printing



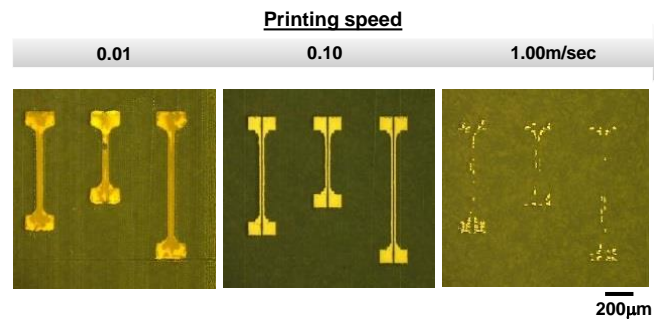
## Current Roll Engraving Technology



## High-Resolution Roll Fabrication



## Printed Volume Fraction



## <2μm Printed Channel

